

Compliance to the code of conduct

I hereby assure that I solve and submit this exam myself under my own name by only using the allowed tools listed below.

Signature or full name if no pen input available

Network Coding

Exam: IN2315 / Endterm Remote **Date:** Thursday 23rd February, 2023
Examiner: Prof. Dr.-Ing. Georg Carle **Time:** 11:30 – 12:45

Working instructions

- This exam consists of **12 pages** with a total of **4 problems**.
Please make sure now that you received a complete copy of the exam.
- The total amount of achievable credits in this exam is 60.5 credits.
- Detaching pages from the exam is prohibited.
- Allowed resources:
 - one cheatsheet (A4, handwritten, both sides)
 - one **non-programmable pocket calculator**
 - one **analog dictionary** English ↔ native language
- Subproblems marked by * can be solved without results of previous subproblems.
- **Answers are only accepted if the solution approach is documented.** Give a reason for each answer unless explicitly stated otherwise in the respective subproblem.
- Do not write with red or green colors nor use pencils.
- Physically turn off all electronic devices, put them into your bag and close the bag.

Problem 1 Multiple Choice (12 credits)

The following subproblems are multiple choice / multiple answer, i. e., at least one answer per subproblem is correct. Subproblems are graded with 1 credit per correct answer and -1 credit per wrong answer. Missing crosses have no influence. The minimal amount of credits per subproblem is 0 credits.

Mark correct answers with a cross



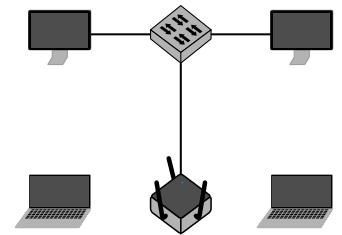
To undo a cross, completely fill out the answer option



To re-mark an option, use a human-readable marking



For Subproblems a) – e) consider the network below, which consists of a wired network with two computers connected to an AP that serves two wireless clients according to IEEE 802.11.



a)* How many broadcast domains does the network contain?

- 3
 6
 1
 5
 2
 4

b)* How many collision domains does the network contain?

- 4
 2
 3
 1
 6
 5

c)* Which of the following statements are true?

- | | |
|---|--|
| <input type="checkbox"/> Computers attached via Ethernet address wireless computers directly. | <input type="checkbox"/> Wireless computers address computers attached via Ethernet directly. |
| <input type="checkbox"/> Wireless computers can differentiate between other wireless clients and computers attached via Ethernet. | <input type="checkbox"/> Wireless computers commonly bypass the AP when communicating with each other. |
| <input type="checkbox"/> Computers attached via Ethernet explicitly address the AP. | <input type="checkbox"/> Computers attached via Ethernet are aware of the AP. |

d)* Assuming random linear network coding with a generation size of $N \geq 4$, the chance that N packets suffice for decoding ...

- | | |
|---|--|
| <input type="checkbox"/> increases exponentially with the number of additional coded packets. | <input type="checkbox"/> primarily depends on the generation size. |
| <input type="checkbox"/> primarily depends on the field size. | <input type="checkbox"/> is above 50 % if GF(2) is used. |
| <input type="checkbox"/> increases linearly with the number of additional coded packets. | <input type="checkbox"/> is roughly 99 % if GF(256) is used. |

e)* Given a network with incidence matrix $M \in \{-1, -0, 1\}^{n \times m}$. Which statements are correct?

- | | |
|--|--|
| <input type="checkbox"/> $\dim \text{null } M = 1$ | <input type="checkbox"/> $M < n$ |
| <input type="checkbox"/> rank M is the number of undirected cycles | <input type="checkbox"/> M^{-1} exists |

f)* Which general statements regarding random linear network coding are correct?

- | | |
|--|--|
| <input type="checkbox"/> Multicast (with replication) can achieve higher flows than coding. | <input type="checkbox"/> The value of a min-cut gives a lower bound for the achievable flow. |
| <input type="checkbox"/> For a two-node packet erasure network, coding cannot achieve higher flows than ARQ. | <input type="checkbox"/> The achievable flow is larger than in routed networks. |
| <input type="checkbox"/> Using pseudo random numbers for coefficients poses a security risk. | <input type="checkbox"/> The flow (according to the min-cut) can always be achieved. |



e) Explain what a reduction polynomial is.

Grid for answer e)



f)* Explain what a primitive element of $F_9[x]$ is.

Box for answer f)

For $x^2 + 1$ as reduction polynomial and $x + 2 \in F_9[x]$ as primitive element we get:

$(x + 2)^0 = 1$	=: 01	$(x + 2)^4 = 2$	=: 02
$(x + 2)^1 = x + 2$	=: 12	$(x + 2)^5 = 2x + 1$	=: 21
$(x + 2)^2 = x$	=: 10	$(x + 2)^6 = 2x$	=: 20
$(x + 2)^3 = 2x + 2$	=: 22	$(x + 2)^7 = x + 1$	=: 11

From these results, we can build the log- and antilog tables:

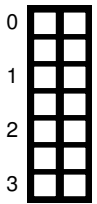
	0	1	2
0			
1			
2			

(a) L

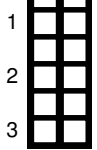
	0	1	2
0			
1			
2			

(b) A

Table 2.1: Log- and antilog tables for $F_9[x]$



g)* State the Antilog table A in Table 2.1.

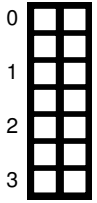


h)* State the Log table L in Table 2.1a.



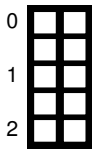
i)* Determine the result of $(x + 1)(2x + 1)$ using the logtable approach.

Grid for answer i)



j)* Verify your result of Subproblem ?? by using the ordinary polynomial division.

Hint: Do not waste too much time in case the results should differ!



Grid for answer j)



For some ξ and a specific FEC scheme we obtain a packet erasure probability of $\varepsilon = 0.1$.



d)* Argue why TCP would not perform as expected under those conditions.

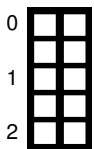
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e) Explain how IEEE 802.11 solves this problem (or at least tries to solve it).

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We now assume that packets are transmitted using (unidirectional) random linear network coding (RLNC) with a generation size of N packets. Let the Galois field in use be sufficiently large such that the influence of random linear dependencies can be neglected. RLNC allows the sender to proactively send enough redundant packets such that on average the receiver will be able to decode.



f)* Explain why this is **impossible** without coding and why this is **possible** with coding.

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g)* Determine the expected number of packets n^* that have to be sent per generation.

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Problem 4 Metrics (17.5 credits)

We consider the wireless network depicted in Figure 4.1 consisting of nodes $N = (s, 1, 2, t)$. Per-node packet erasure probabilities are given $\forall i, j \in N$ as $0 \leq \epsilon_{ij} \leq 1$ and $i \neq j$. Erasures are assumed to be independently and identically distributed.

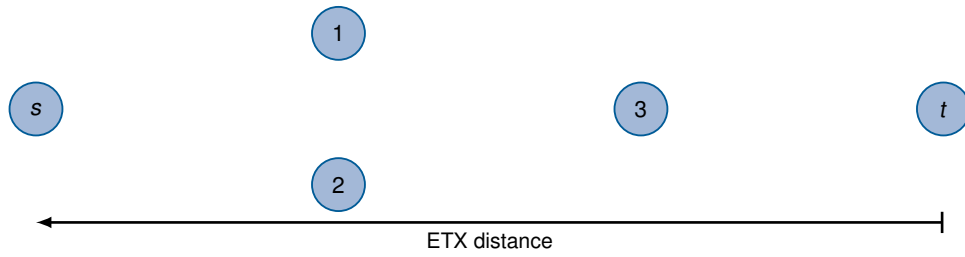


Figure 4.1: Wireless network, all hyperarcs are assumed to exist.

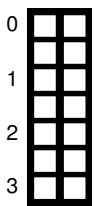
Note that Nodes 1 and 2 have the same ETX distance to the destination.



a)* Briefly explain the ETX distance between s and t .



b)* Argue which distribution the individual terms of the ETX metric adhere to.



c)* Derive the ETX distance d_{st}^{ETX} as used by MORE.

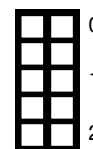
In the following, we consider the EOTX metric and want to derive the amount of packets individual nodes have to transmit per source packet. To this end, we need the

$$R_j = \sum_{i>j} z_i(1 - \epsilon_{ij}), \quad (4.1)$$

$$L_j = \sum_{i>j} \left(z_i(1 - \epsilon_{ij}) \prod_{k<j} \epsilon_{ik} \right), \text{ and} \quad (4.2)$$

$$z_j = \frac{L_j}{1 - \prod_{k<j} \epsilon_{jk}}. \quad (4.3)$$

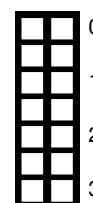
d)* Which factor does the EOTX metric consider that is not considered by the ETX metric? Give a concrete example based on Figure 4.1.

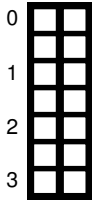


e)* Explain R_j as given in (4.1).

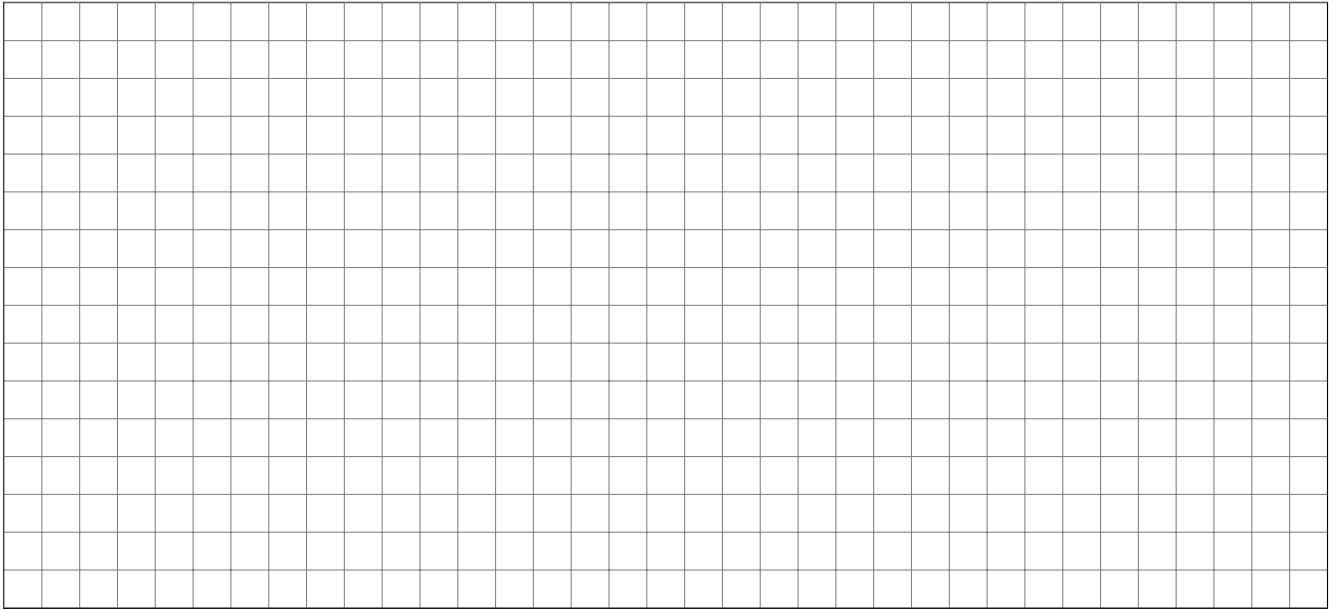


f)* Derive R_j for $j \in \{1, 2, 3, t\}$. Note that $R_s = 1$.

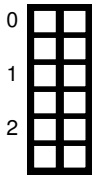




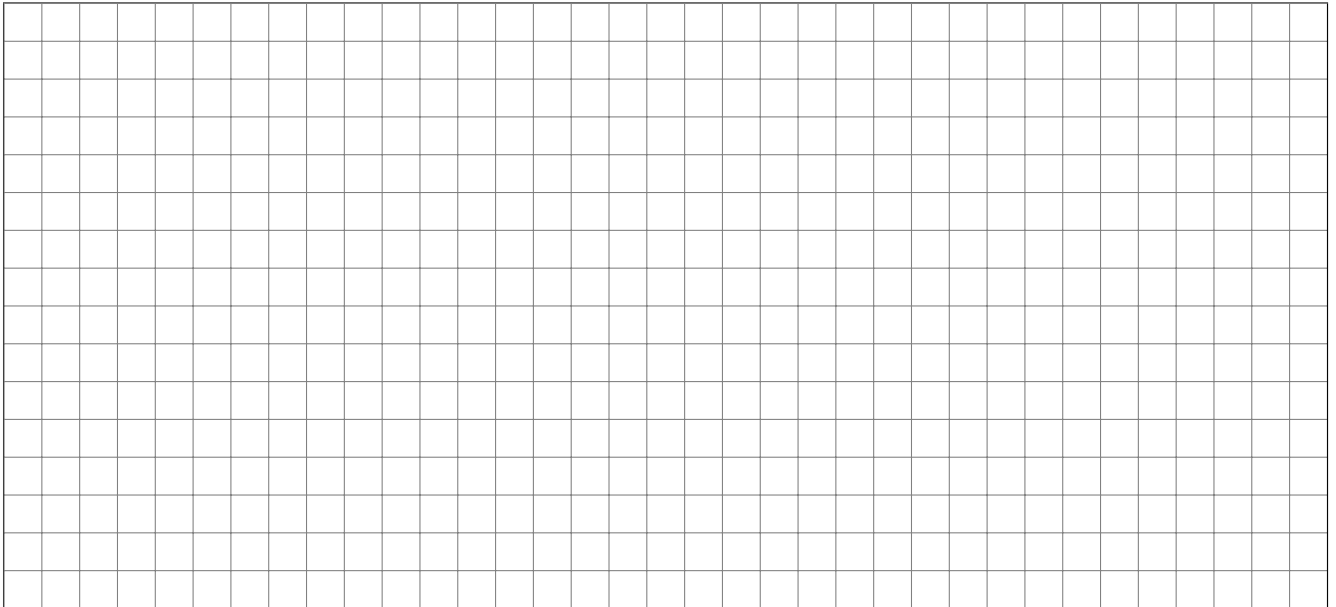
g)* Derive L_j for $j \in N$.



h)* Explain z_j as given in (4.3).



i) Derive z_j for $j \in N$.



Additional space for solutions—clearly mark the (sub)problem your answers are related to and strike out invalid solutions.

